lago: Al Driven Superoptimization for LLVM



Manasij Mukherjee NVIDIA John Regehr University of Utah

Talk Organization

Motivation

Why solve this problem?

Design

What worked and what doesn't?

Results

How well does it work?

What is Superoptimization?

Can a piece of code be improved?

Specifically, by **searching** for a refinement.

```
define i32 @foo(i32 %x) {
entry:
  %a = and i32 %x, 1431655765
  %b = 1 shr i32 %x, 1
  c = and i32 %b, 1431655765
  %d = add i32 %a, %c
  e = and i32 %d, 858993459
  %f = 1shr i32 %d, 2
  %g = and i32 %f, 858993459
  %h = add i32 %e, %g
  %i = and i32 %h, 252645135
  %j = 1shr i32 %h, 4
  %k = and i32 %j, 252645135
  %1 = add i32 %i, %k
  m = and i32 %1, 16711935
  %n = 1 shr i32 %1, 8
  %o = and i32 %n, 16711935
  p = add i32 %m, %o
  q = and i32 p, 65535
  %r = 1 shr i 32 %p, 16
  %s = and i32 %r, 65535
  %t = add i32 %q, %s
  ret i32 %t
```

Searching for a refinement

Enumerate a bunch of candidates

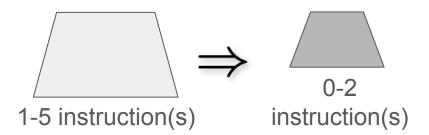


Attempt to verify each

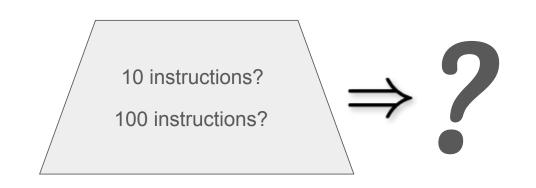
Superoptimizing sqlite3 (53.94k lines of code) takes ~24 hours with 128 cores with **Souper**

What's on the table?

What we usually put into InstCombine today:

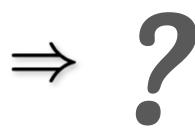


One off pattern in your important code that is not generally useful



```
define i32 @foo(i32 %x) {
entry:
  %a = and i32 %x, 1431655765
  %b = 1 shr i32 %x, 1
  c = and i32 %b, 1431655765
  %d = add i32 %a, %c
  e = and i32 %d, 858993459
  %f = lshr i32 %d, 2
  %q = and i32 %f, 858993459
  %h = add i32 %e, %g
  %i = and i32 %h, 252645135
  %j = 1shr i32 %h, 4
  %k = and i32 %j, 252645135
  %1 = add i32 %i, %k
  m = and i32 %1, 16711935
  %n = 1 shr i32 %1, 8
  %o = and i32 %n, 16711935
  p = add i32 m, %0
  q = and i32 p, 65535
  %r = 1 shr i 32 %p, 16
  %s = and i32 %r, 65535
  %t = add i32 %q, %s
  ret i32 %t
```

Do we really need to optimize long sequences?



Superoptimization examples

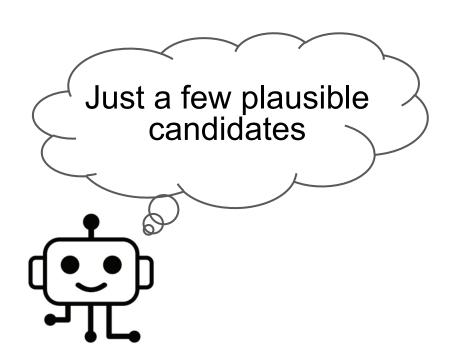
```
define i32 @foo(i32 %x) {
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 %1 = add i32 %i, %k
 m = and i32 %1, 16711935
 %n = 1 shr i32 %1, 8
 %o = and i32 %n, 16711935
 %p = add i32 %m, %o
 %q = and i32 %p, 65535
 r = 1 shr i32 p, 16
 %s = and i32 %r, 65535
 %t = add i32 %g, %s
 ret i32 %t
```

ctpop %x

```
define i32 @src(i1 %c) {
  %8 = zext i1 %c to i32
  %9 = select i1 %c, i32 2, i32 0
  %10 = \text{ or } i32 \%8, \%9
  %11 = select i1 %c, i32 4, i32 0
  %12 = \text{ or } i32 %10, %11
  %13 = select i1 %c, i32 8, i32 0
  %14 = \text{ or } i32 %12, %13
  %15 = select i1 %c, i32 256, i32 0
  %16 = or i32 %14, %15
  %17 = select i1 %c, i32 512, i32 0
  %18 = or i32 %16, %17
  %19 = select i1 %c, i32 1024, i32 0
  %20 = \text{ or } i32 %18, %19
  %21 = select i1 %c, i32 2048, i32 0
  22 = \text{ or } 32 20, 21
  ret i32 %22
```

select i1 %c, i32 3855, i32 0

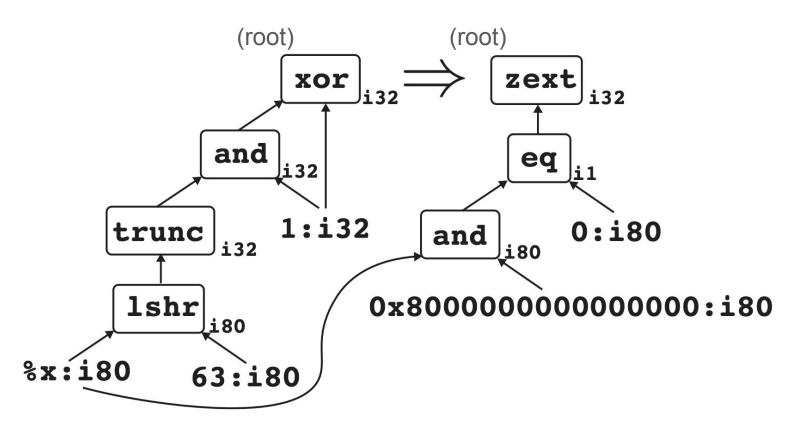
Why replace the enumeration with AI?



Reach far deeper into the search space

Attempt to verify each

Example - guess what this is!



Superoptimization → Compilers

Can a piece of code be improved?

Can we improve the compiler such that -

Hydra

it improves this piece of code?

... it improves other, similar, pieces of code?

... and does not regress anything else?

Talk Organization

Motivation

Why solve this problem?

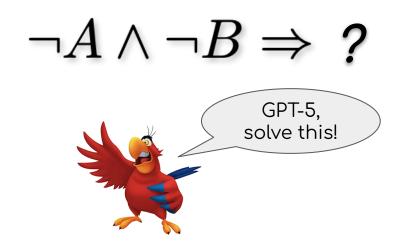
Design

What worked and what doesn't?

Results

How well does it work?

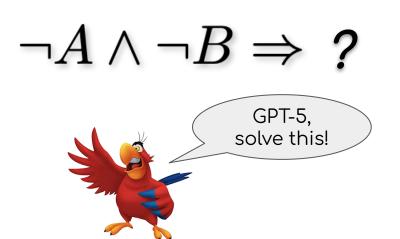
Baseline: just asking the LLM!





The expression you've given seems to be an incomplete logical expression. The "=>" symbol typically indicates implication, suggesting that ...

Two significant issues





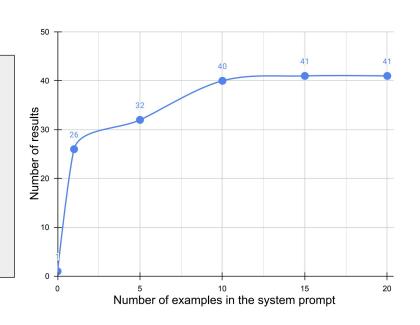
The expression you've given seems to be an incomplete logical expression. The "=>" symbol typically indicates implication, suggesting that ...

Wrong syntax!

Wrong semantics!

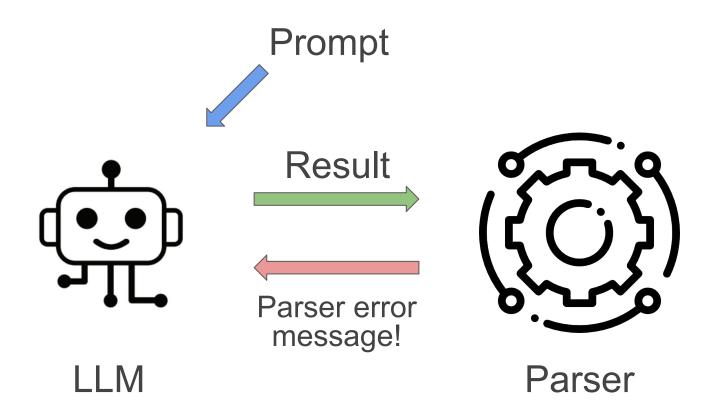
lago's System Prompt

- Explain the idea of peephole optimizations
- Describe available operations
- Negative statements about what to avoid
- Examples



No correctness guarantee from an LLM

Getting the right syntax



Fixing seemingly consistent issues

LLM results kept redefining values

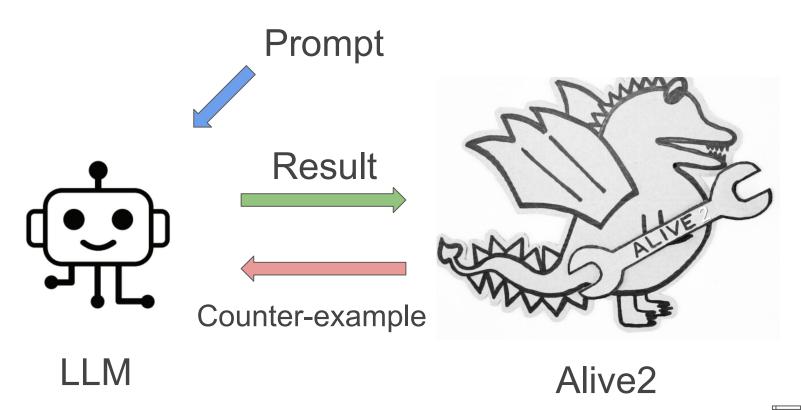
```
%x = add i32 %a, %b
%x = add i32 %x, 1

%x = add i32 %a, %b
%x' = add i32 %x, 1
```

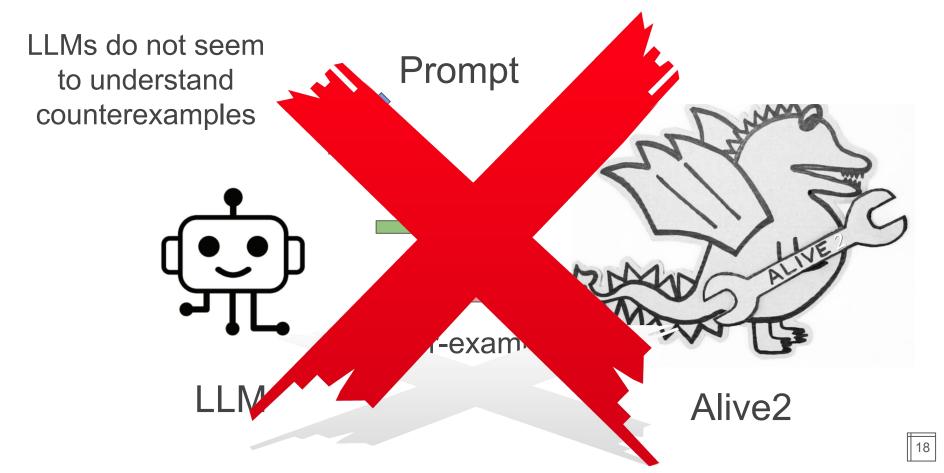
Wrong types

Insert appropriate icmp or trunc

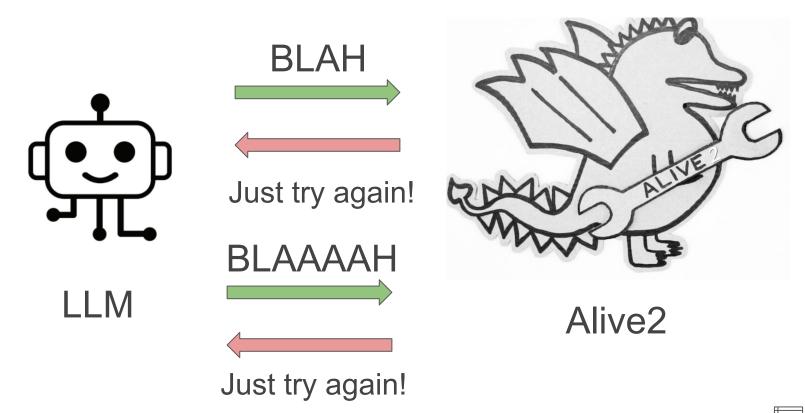
What about correctness?



Does not work, at all.



Works, sort of...



Can we do better?

Formal Methods to the rescue again!



$$\neg A \land \neg B \Rightarrow$$
 ?

No correctness guarantee from an LLM

Verify Results

with

Alive2 + Z3

Fix Results

with

CEGIS

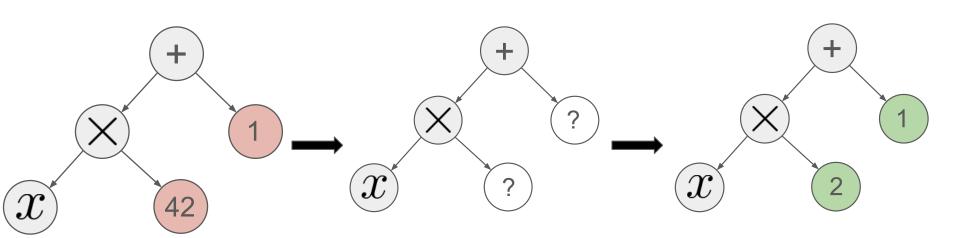




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Fixing Incorrect Results

Extract a sketch



Fill in the blanks with an SMT solver

How do we fill in the blanks with an SMT solver?

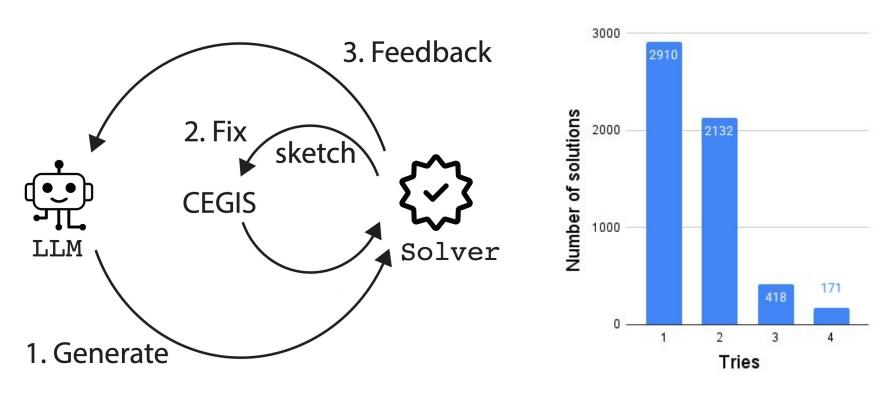
This is the logical formula in question

$$\exists C. \forall x. f(x, C) = g(x, C)$$

Counterexample Guided Inductive Synthesis

Solving Exists/Forall Problems With Yices [Dutertre]

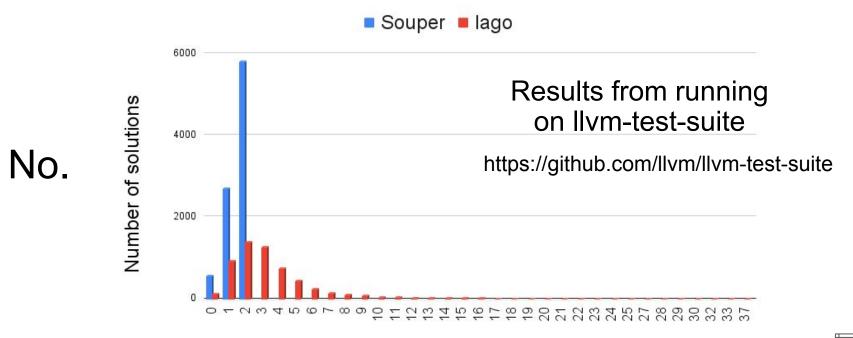
Recap: lago's Synthesis Loops



All results formally verified

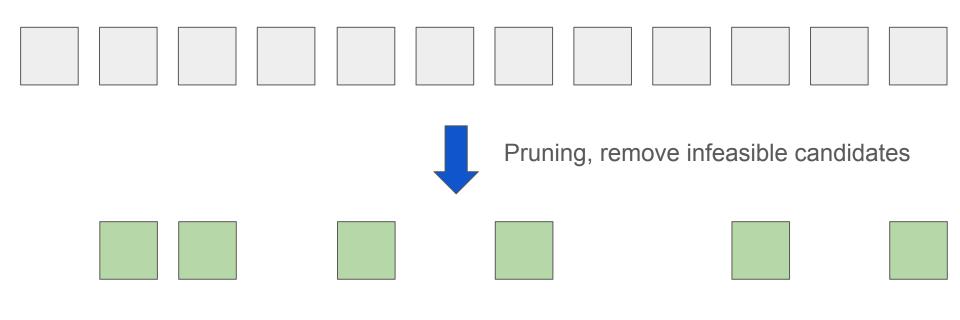
What about completeness?

Can we guarantee finding a refinement if one exists?



Towards Completeness

First level of search tree, incomplete candidates.



Fits in an LLM context window now!

lago is sound but not complete.

Monkey's Paw

We have wished for:

Correct syntax

Must be a valid refinement

```
x == y \models
(x & \sim y) == 0
x == y
```

```
%0:i64 = var
%1:i64 = var
%2:i64 = xor -1:i64, %1
%3:i64 = and %0, %2
%4:i1 = eq 0:i64, %3
infer %4
%5:i1 = eq %0, %1
pc %5 1:i1
result %5
```

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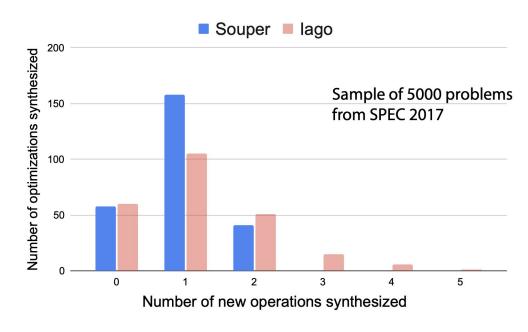
How well does it work?

lago results summary

More complex optimizations, complements Souper.

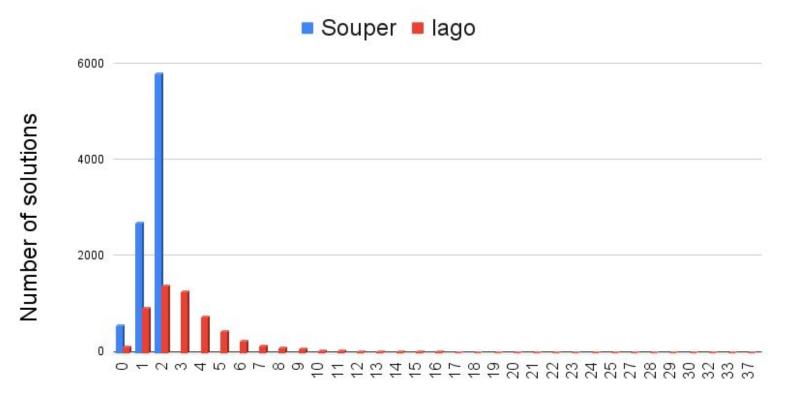
35.7% results are new!

7.4% fewer total results



Results on Ilvm-test-suite

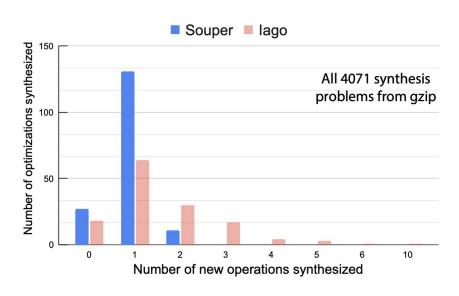
https://github.com/llvm/llvm-test-suite

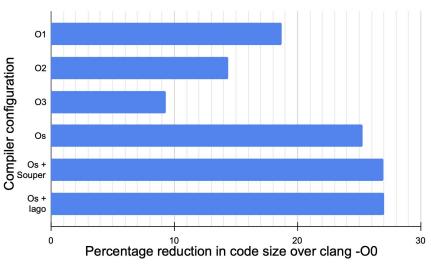


lago results summary

Finds optimizations in gzip a 30 year old codebase.

Matches Souper's code size reduction for gzip

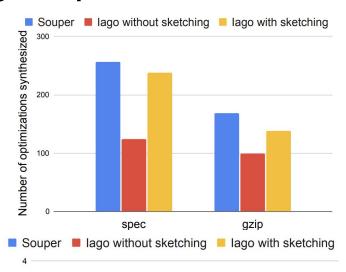


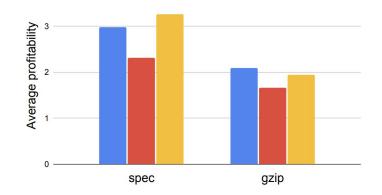


Does sketching help?

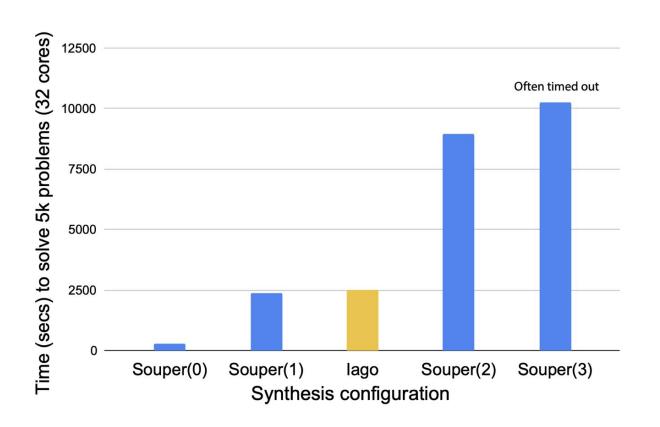
More results

More profitable results

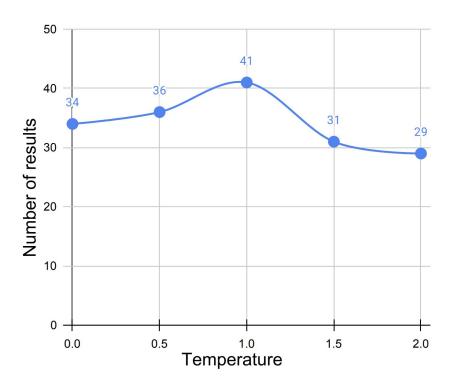




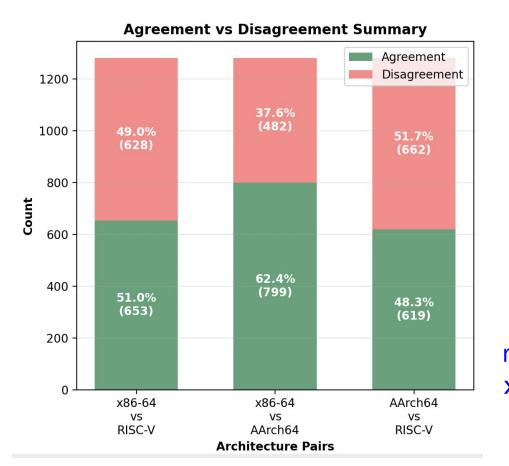
Is it faster than Souper?

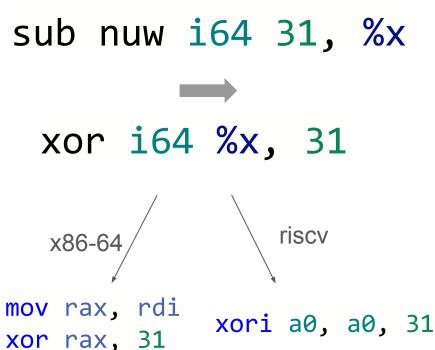


GPT-4 Temperature Parameter

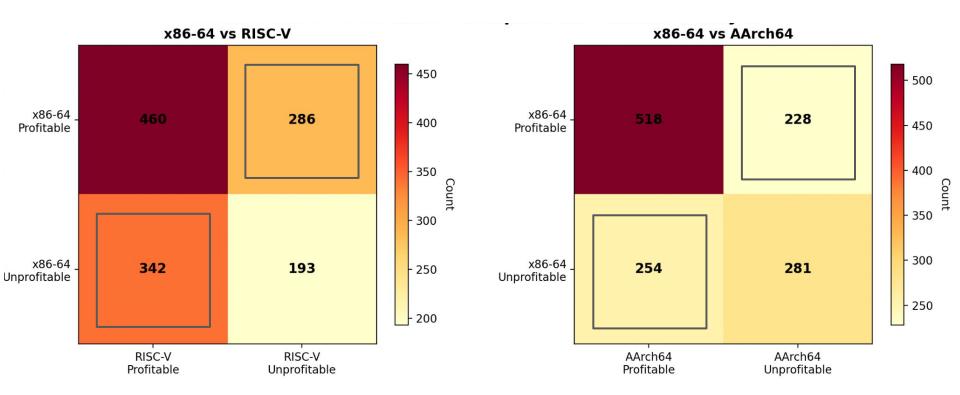


Do different backends agree on lago's optimizations?





Breakdown - x86-64 vs RISC-V and x86-64 vs AArch64



Profitable in this context - produces fewer asm instructions

Takeaways implementing these optimizations

```
define i32 @src(i1 %c) {
  %8 = zext i1 %c to i32
  %9 = select i1 %c, i32 2, i32 0
  %10 = \text{ or } i32 \%8, \%9
  %11 = select i1 %c, i32 4, i32 0
  %12 = \text{ or } i32 %10, %11
  %13 = select i1 %c, i32 8, i32 0
  %14 = \text{ or } i32 \%12, \%13
  %15 = select i1 %c, i32 256, i32 0
  %16 = or i32 %14, %15
  %17 = select i1 %c, i32 512, i32 0
  %18 = or i32 %16, %17
  %19 = select i1 %c, i32 1024, i32 0
  %20 = \text{ or } i32 \%18, \%19
  %21 = select i1 %c, i32 2048, i32 0
  %22 = \text{ or } i32 \%20, \%21
  ret i32 %22
```

Often multiple transforms in disguise

```
define i32 @tgt(i1 %c) #0 {
    %8 = select i1 %c, i32 3855, i32 0
    ret i32 %8
}
```

Takeaways

Takeaways implementing these optimizations

Conflicts with canonicalization

Termination issues! zext(xor 1:i1, b:i1) => 1 - zext(b)

Picking the right subset is tricky

Symbiosis between Al

and

Formal Methods

Great at generating text

No correctness guarantees



Exhaustive synthesis

Always correct

Some final - REDO

```
src:
                           andi
                                  a0, a0, 255
                           slli
                                  a0, a0, 3
!(x0:i8 < u 9)
                           addi
                                  a0, a0, -65
  |=
                          slli
                                  a0, a0, 32
zext(((zext(x0) << nw 3)
                           srli
                                  a0, a0, 32
 +nsw 0xFFFFFBF))
 =>
                         tgt:
                           andi
                                  a0, a0, 255
(zext(x0) \ll 3)
                           slli
                                  a0, a0, 3
 addi
                                  a0, a0, -65
```

```
src:
(trunc((x0:i80 >> 1 63))
                                       rax, rdi
                               mov
 & 1) ^ 1
                               shr
                                       rax, 63
  =>
                               xor
                                       eax, 1
zext((
                             tgt:
 (x0 & 0x8000000000000000)
                               xor
                                       eax, eax
  == 0))
                               bt
                                       rdi, 63
                                       al
                               setae
```

```
src:
                              mov
                                      eax, edi
                                      ecx, edi
                              mov
                                      edx, edx
                              xor
                              div
                                      esi
zext(x:i32) -
                                      rcx, rdx
                              sub
  zext((x %u y:i32))
                              mov
                                      rax, rcx
    =>
                            tgt:
zext((x - (x %u y)))
                                      eax, edi
                              mov
                                      edx, edx
                              xor
                              div
                                      esi
                              sub
                                      edi, edx
                                      rax, rdi
                              mov
```



Takeaways

Al for compiler work - Trust, but verify.

Formal methods to verify and fix results.



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